

Stability and Transitions in Emerging Market Policy Rules

Author(s): ASHIMA GOYAL and SHRUTI TRIPATHI

Source: *Indian Economic Review*, Vol. 49, No. 2 (July - December 2014), pp. 153-171

Published by: Department of Economics, Delhi School of Economics, University of Delhi

Stable URL: <http://www.jstor.org/stable/24725790>

Accessed: 11-01-2018 05:12 UTC

---

JSTOR is a not-for-profit service that helps scholars, researchers, and students discover, use, and build upon a wide range of content in a trusted digital archive. We use information technology and tools to increase productivity and facilitate new forms of scholarship. For more information about JSTOR, please contact [support@jstor.org](mailto:support@jstor.org).

Your use of the JSTOR archive indicates your acceptance of the Terms & Conditions of Use, available at <http://about.jstor.org/terms>



JSTOR

*Department of Economics, Delhi School of Economics, University of Delhi is collaborating with JSTOR to digitize, preserve and extend access to Indian Economic Review*

## Stability and Transitions in Emerging Market Policy Rules

ASHIMA GOYAL<sup>1</sup>

*Indira Gandhi Institute of Development Research, Mumbai*

AND

SHRUTI TRIPATHI

*National Institute of Public Finance and Policy, Delhi*

### ABSTRACT

Conditions for stability in an open economy dynamic stochastic general equilibrium model adapted to a dualistic labor market (SOEME) are the same as for a mature economy. But the introduction of monetary policy transmission lags makes it deviate from the Taylor Principle. Under rational expectations a policy rule is unstable, but under adaptive expectations traditional stabilization gives a determinate path, with weights on the objective of less than unity. Estimation of a Taylor rule for India and optimization in the SOEME model itself, all confirm the low weights. The results imply that under rational expectations, optimization is better than following a rule. If backward looking-behavior dominates, however, a policy rule can prevent overshooting and instability. Economy-specific rigidities must inform policy design, and the appropriate design will change as the economy develops.

**Keywords:** DSGE; Emerging Market; Rigidities; Stability; Optimization; Taylor Rule

**JEL Classification:** E26, E52

### 1. INTRODUCTION

We examine stability and determinacy in a dynamic stochastic general equilibrium (DSGE) model for a small open economy (SOE), adapted to an emerging market (SOEME) with two types of consumer-workers. One group has high and the other low productivity<sup>2</sup>. Stability results have the same structure as in the SOE.

In the calibrated SOEME model, however, some transmission lags and some degree of backward-looking behavior are necessary to reproduce data moments for an emerging market (EM). With these changes, policy optimization solving for macro variables as a function of expected future value delivers stability and determinacy at lower output cost. Coefficients of the policy reaction function are low. But a monetary rule requires

---

<sup>1</sup> Corresponding Author: Indira Gandhi Institute of Development Research, Gen. Vaidya Marg, Santosh Nagar, Goregaon (E), Mumbai-400 065. Email: ashima @ igidr.ac.in.

*Acknowledgments:* The paper is a revised version of IGIDR WP-2012-004. An earlier version was presented at the ISI Delhi Annual Conference. We thank the participants for comments and Reshma Aguiar for help with the word processing.

<sup>2</sup> See Goyal (2011), who extends Galí and Monacelli (2005) to such an emerging market.

unrealistic weights for stability. This implies discretionary optimization is more effective than following a monetary policy rule if agents are forward-looking.

A rule-based traditional stabilization where agents solve current variables as a function of past data turns out to require low weights on both inflation and the output gap for stability. The weights fall with a rise in the share of forward-looking behavior. A rule can, therefore, be followed, if backward-looking behavior dominates, but its coefficients should not exceed unity. Then it contributes to stability by preventing over- or under-shooting of policy rates.

In an EM with delayed transmission of policy rates, stability turns out to be very sensitive to the share of forward-looking behavior. This suggests volatility can be high if policy rules are followed unless weights are kept low. Such a policy rule contributes to stability since it prevents over- or under-shooting due to lagged effect of policy.

These results imply that the coefficients of a policy rule in an EM should change as monetary transmission matures and behavior becomes more forward-looking. During transition, discretionary optimization may offer more flexibility, and the Taylor Principle that the weight on inflation in a policy rule must exceed unity does not hold. The results may apply more generally than to EMs alone since other economies also have various types of frictions.

The practice of monetary policy in India is consistent with these results. The Central Bank's reaction function in the calibrated SOEME, and a monetary policy rule estimated with Indian data both show response coefficients much smaller than unity. Thus, during the estimation period, policy avoided the instability that the Taylor Principle could entail in Indian conditions.

The structure of the paper is as follows: Section 2 places the SOEME stability issues in the relevant literature; Section 3 presents the basic SOEME model; Section 4 derives the implications of stability for a policy rule; Section 5 develops the adaptive expectations case; Section 6 presents an estimated monetary policy rule, before Section 7 concludes.

## 2. LITERATURE REVIEW

Models with forward-looking behavior can have nominal explosions. Sargent and Wallace (1975) demonstrated that with rational expectations inflation is indeterminate under an interest rate instrument. Since there is no effective nominal anchor, inflation can take many values. But McCallum (1981) later showed such indeterminacy only occurs if the Central Bank (CB) places no weight on inflation in its response. The CB response to inflation, or its targeting of nominal money stock, can provide the nominal anchor required to fix the price level or inflation. In addition, other rigidities and lags may serve to anchor inflation (Friedman, 1990).

It is shown analytically, in the canonical NKE forward-looking model (Woodford, 2003) that a CB response to inflation above target exceeding unity selects the unique saddle-stable inflation path thus ensuring determinacy. Since there is a unique stable path, rational expectations converge to this. It ensures stability since it rules out explosive nominal paths of self-fulfilling inflation expectations. If for each one-percent increase in inflation, the central bank raises the nominal interest rate by more than one percentage point (Taylor 1993, p. 202) the policy rate adjusts more than one-to-one with inflation. This is known as the Taylor Principle and eventually implies positive real interest rates.

Evans and Honkapohja (2003) make the point that such a policy rule works because it conditions the policy response not only on inflation but also on individuals' expectations. It contributes to stability since outcomes depend on these expectations.

This literature justifies a Taylor type monetary policy rule with a weight on inflation greater than unity, showing that it can perform as well as discretionary optimization. A rule can also be justified as a credible commitment, preventing opportunistic behavior that results in an inflation bias. In emerging democracies where inflation hurts the poor and loses votes, however, CBs may not have an inflation bias (Goyal, 2007)<sup>3</sup>.

But, further work, surveyed in Galí *et al.* (2004) shows monetary policy rules are fragile and sensitive to the assumptions of the model. Such rules can be a source of instability. A large literature on monetary policy rules under adaptive learning followed seminal work by Evans and Honkapohja (2003). It generally shows rules that generate determinate equilibrium also lead to expectational stability (E-stability) under learning (Bullard and Mitra, 2002), so that expectations are not perfectly rational. But again regions of determinacy are sensitive to model assumptions and parameters.

How does our model fit in and contribute to the literature? Like the learning literature, we explore non-rational expectations, but we also consider the case where the share of backward-looking behavior is large enough to analyze a traditional stabilization, rather than rational expectations equilibrium. The learning literature stays with the latter. Thus, we also consider a pure backward-looking equilibrium.

Our results support the general finding of fragility and context-specificity of policy rules and of the Taylor principle. But show this in the context of a dualistic EM not yet addressed in the literature. In Galí *et al.* (2004), a share of rule-of-thumb consumers implies demand rises with output, requiring a higher weight on inflation for stability. Our model differs in that subsistence consumption is given exogenously and so demand does not rise with output. Our aggregate demand equation, therefore, differs from theirs.

---

3 Clarida *et al.* (1999) point out, however, in a discretionary optimum also, even though the CB re-optimizes every period, it may not have an incentive to deviate and create surprise inflation, and the private sector recognizes this.

The literature has also explored the role of inertia and lags. Bullard and Mitra (2007) add interest rate stabilization or a lagged interest rate term in the policy rule and show that this raises the region of determinacy and learning. Duffy and Xiao (2007) have a similar result. We have such an interest stabilization term, but the rational expectations equilibrium is still indeterminate in our model if the Taylor Principle is followed.

Evans and McGough (2005) have lagged inflation and output terms in the AS and AD curves respectively and find these do not affect the indeterminacy result, which continues to prevail. New regions of explosiveness are added. We have a lagged inflation term, but add a lagged interest rate term in the AD to capture market segmentation that delays policy transmission. The literature does not, to our knowledge, as yet explore the effect of such a term. We find that this combination of lags erodes the existence of a unique rational expectations equilibria.

Another new result is a high share of backward-looking behavior can justify a policy rule with low weights. But the presence of some forward-looking behavior makes the equilibrium determinate for some parameter combinations leading to a unique equilibrium.

Our result, therefore, offers a response to Cochrane (2011)'s criticism of the NKE determinacy result that it requires unrealistic CB behavior on out of equilibrium paths. On such explosive paths, higher inflation requires CBs to raise expected inflation even more in order to switch expectations to the unique path as against the old Keynesian stabilizing logic of raising interest rates to reduce demand and, therefore, inflation. On an explosive path, for example, real rates can fall with inflation, and create more inflation as money supply rises under an interest rate rule. Such expected policy reactions cannot apply in a stabilizing solution based on past behavior. But there is a unique stable path, so the ad hoc charge that applies to old Keynesian stabilization is not valid. Instability occurs, however, with large policy responses due to overshooting of policy rates in the presence of lags. This is known as instrument instability.

The above argument also gives a justification for the empirical estimation of a policy rule. Cochrane (2011) argues that a monetary policy rule is not identified under rational expectations. Since variables jump to a unique path, the adjustment process cannot be estimated. What are estimated are correlations in shocks that shift inflation to a unique equilibrium. The criticism does not hold for past-based adjustment paths with smoothing.

Since the objective is to explore stability in the specific context of a dualistic EM with transmission lags and draw implications for policy, we do not analyze different types of policy rules, and other issues, which are already examined in the literature (Bullard and Mitra 2002).

After a brief description of the SOEME model, we turn to stability results.

### 3. A SMALL OPEN EMERGING MARKET MODEL

A microfounded dynamic stochastic general equilibrium (DSGE) model for a small open emerging market is used to derive the aggregate demand (AD) (2) and aggregate supply (AS) (3)<sup>4</sup>. The central bank (CB) minimizes a loss function (1), based on consumers' welfare and a desire for smoothing, subject to (2) and (3). The loss function is a weighted average of output, inflation and interest rate deviations from equilibrium values:

$$L = q_x x_t^2 + q_\pi \pi_t^2 + q_i i_t^2 \quad \dots(1)$$

The last term captures the smoothing preferences that prevent large changes in the policy rate, where  $i_t$  is the riskless nominal interest rate. The first term is the output gap  $x_t = y_t - \bar{y}_t$ , and the second term, inflation, can be either consumer price inflation  $\pi_t \equiv p_t - p_{t-1}$  (where price  $p_t \equiv \log P_t$ ) or domestic inflation  $\pi_{H,t}$ . Lower case letters are logs of the respective variables. Table 1 explains the parameters and gives their calibrated values.

The AD and AS are derived from forward-looking consumer and firm optimization respectively, in a dualistic structure with two types  $R$  and  $P$  of consumer-workers. The  $R$  types, with population share  $\eta$ ,  $0 < \eta < 1$ , are able to smooth consumption at international levels in perfect capital markets.  $P$  types are assumed to be at a subsistence consumption  $c_p$ , financed by transfers from  $R$  types mediated by the government. Subsistence consumption changes exogenously. The labour supply elasticities of the  $P$  types are higher than those of the  $R$  types and for the  $P$  type intertemporal elasticity of consumption is zero.

---

4 The derivations are available in Goyal (2011).

TABLE 1  
BENCHMARK CALIBRATIONS

<i>Baseline Calibrations</i>		
Degree of price stickiness	$\theta$	0.75
Price response to output	$\varphi$	0.25
Labour supply elasticity of P type	$\varphi_P$	0.01
Labour supply elasticity of R type	$\varphi_R$	0.6
Elasticity of substitution between differentiated goods	$\varepsilon$	6
Steady state real interest rate or natural interest rate	$\bar{\rho}$ or $\bar{i}$	0.01
Variations in the natural interest rate due to temporary shocks	$\bar{rr}$	$0.01 \pm$
Degree of openness	$\alpha$	0.3
Proportion of the R type	$\eta$	0.4
The intertemporal elasticity of substitution of the R type	$1/\sigma_R$	1
The intertemporal elasticity of substitution of the P type	$1/\sigma_P$	0
Consumption of the P type	$C_P$	0.2
Consumption of the R type	$C_R$	1
Share of backward looking price setting	$\gamma_b$	0.2
Share of forward looking price setting	$\gamma_f$	0.8
Weight of output in the CB's loss function	$q_y$	0.7
Weight of inflation in the CB's loss function	$q_\pi$	2
Weight of the interest rate in the CB's loss function	$q_i$	1
<i>Implied parameters</i>		
Weighted average elasticity of substitution	$1/\sigma_D$	0.58
Discount factor	$\beta$	0.99
Weighted average consumption level	$C$	0.75
Log deviation from world output	$\kappa$	0.1
Philips curve parameter	$\lambda$	0.24
Steady state real interest rate, discount rate	$\rho$	0.01
Labour supply elasticity	$1/\varphi$	4
<i>Shocks</i>		
Persistence of natural rate shock	$\rho^r$	0.75
Persistence of cost-push shock	$\rho^c$	0
Standard deviation of natural rate shock	$\sigma_\varepsilon^r$	0.01
Standard deviation of cost-push shock	$\sigma_\varepsilon^c$	0.2

The dynamic AD equation for the SOEME is:

$$x_t = E_t\{x_{t+1}\} - \frac{1}{\sigma_D}(i_t - E_t\{\pi_{H,t+1}\} - \bar{rr}_t) \quad \dots(2)$$

where:  $\overline{rr}_t = \rho - \sigma_D \Gamma(1 - \rho_a) a_t - \sigma_D(1 - \eta + \Phi) E_t \{\Delta c_{P, t+1}\} + \sigma_D(\Theta - \Psi) E_t \{\Delta y_{t+1}^*\}$

$$\Theta = \alpha(\varpi - \eta) \quad , \quad d = \frac{1}{\sigma_D + \varphi} \quad , \quad \Gamma = \frac{(1 + \varphi)}{\sigma_D + \varphi} \quad , \quad \Psi = \eta(\sigma - \sigma_D)d$$

$$\sigma_D = \frac{\sigma_R}{(\eta(1 - \alpha) + \varpi\alpha)} \quad , \quad \Phi = d((1 - \eta)(\sigma - \sigma_D)) \quad , \quad \varpi = \sigma_R + (1 - \alpha)(\sigma_R - 1)$$

The steady-state natural interest rate,  $\rho$ , is defined as the equilibrium real rate, consistent with a zero or target rate of inflation, when prices are fully flexible. It is also the time discount rate since  $\rho \equiv \beta^{-1} - 1 = -\log \beta$  where  $\beta$  is the discount factor. Shocks that change the natural rate open an output gap and affect inflation. The term  $\overline{rr}_t$  that enters the AD, therefore, captures deviation of the natural rate from its steady-state value. The deviation occurs due to real disturbances that change natural output;  $\overline{rr}_t$  rises for any temporary demand shock and falls for any temporary supply shock. Optimal policy requires insulating the output gap from these shocks, so that the CB's interest rate instrument moves in step with the natural rate. Thus, the CB would accommodate positive supply shocks that raise the natural output by lowering interest rates. It would offset positive demand shocks that raise output above its potential by raising interest rates. Full stabilization at the current natural output implies that  $x_t = \pi_{H, t} = 0$ ,  $y_t = \overline{y}_t$  and  $r_t = \overline{rr}_t$ .

In an EM a change in  $c_p$  is an additional shock. A fall requires reduction in the policy rate, since it increases willingness to work of  $P$  type workers. The distance from the world consumption level also rises. The parameters of the other shock terms also differ from those for the SOE. Since productivity shocks,  $a_p$ , can be more persistent in EMs that are in transition stages of upgrading technologies, they change the natural rate less. A temporary shock to  $c_p$  turns out to have the largest effect on the natural rate (Goyal 2009).

The dynamic AS is:

$$\pi_{H, t} = \gamma_f \beta E_t \{\pi_{H, t+1}\} + \kappa_D x_t + \gamma_b \pi_{H, t-1}, \text{ where } \gamma_f + \gamma_b = 1 \quad \dots(3)$$

The response of inflation to the output gap is  $\kappa_D = \lambda(\sigma_D + \varphi)$ . Since both empirical estimations and the dominance of administered pricing in an EM suggest that past inflation affects current inflation, the AS (3) has a positive  $\gamma_b$  as the share of lagged, and  $\gamma_f$  as the share of forward-looking inflation.

Marginal cost at its steady-state level, when prices are perfectly flexible, defines the natural output  $\overline{y}_t$ . But the world output level is the final steady-state for a SOEME. Low productivity, poor infrastructure and other distortions keep the natural output in an EM

below world levels. Convergence to world output levels for all the SOEME population is part of the process of development. Goyal (2011) systematically compares the differences in behavior and outcomes for the SOE and SOEME. As  $\eta$  approaches unity, the EM becomes developed and the SOEME converges to the Galí and Monacelli (2005) (GM) type SOE with per capita consumption reaching the normalized world level of unity.

In the next section we analyze the stability properties of the SOEME. In NKE-SOE models a Taylor-type policy rule imposes stability in the rational expectations solution. An equivalent rule can be derived for a basic SOEME model. Since the two models have a similar structure, they differ only in parameter values. The policy response coefficient to inflation turns out to exceed unity in both models.

#### 4. WHAT STABILITY IMPLIES FOR A POLICY RULE

As in the SOE system, the SOEME system comprising (2) and (3) is unstable under forward-looking optimization solving for endogenous variables as a function of expected future values. To see this, substitute dynamic AD (2) in the AS<sup>5</sup> (3) to write the AS as a function of  $x_{t+1}$ . The two equations then become:

$$x_t = E_t \{x_{t+1}\} + \sigma_D^{-1} E_t \{\pi_{H,t+1}\} \quad \dots(4)$$

$$\pi_{H,t} = \kappa_D E_t \{x_{t+1}\} + (\beta + \sigma_D^{-1} \kappa_D) E_t \{\pi_{H,t+1}\} \quad \dots(5)$$

In matrix form they are:

$$\begin{bmatrix} x_t \\ \pi_t \end{bmatrix} = A_o \begin{bmatrix} E_t \{x_{t+1}\} \\ E_t \{\pi_{t+1}\} \end{bmatrix} \text{ and } A_o \equiv \begin{bmatrix} 1 & \sigma_D^{-1} \\ \kappa_D & \beta + \kappa \sigma_D^{-1} \end{bmatrix} \quad \dots(6)$$

Since the determinant and trace of the coefficient matrix  $A_o$  are both greater than zero, the system is unstable. There is local indeterminacy. Sunspot explosions can occur.

Woodford's (2001) result was that interest rate rules lead to indeterminacy of the rational expectations consistent price level only if the path of the short-term policy rate is exogenous. In particular, determinacy requires the Taylor Principle to be satisfied, since it implies that the policy rate reacts to inflation.

We derive the equivalent stability condition for the simplified SOEME. A Taylor-type policy rule whereby the interest rate is raised if there is domestic inflation or if the output gap is positive is:

$$i_t = \bar{r}r_t + \phi_\pi \pi_{H,t} + \phi_x x_t \quad \dots(7)$$

Substituting for  $i_t$  minus its equilibrium value from the policy rule (7) into (2), transforming

<sup>5</sup> We consider the simplest version of the SOEME so  $\gamma_f$  is taken as equal to 1.

$\pi_{H,t}$  into  $\pi_t$ , substituting for  $\pi_t$ , then substituting for  $x_t$  with  $i_t$  substituted in it, in (3), we get:

$$(\sigma_D + \phi_x + \phi_\pi \kappa_D) x_t = \sigma_D E_t \{x_{t+1}\} + (1 - \phi_\pi \beta) - \phi_\pi \beta E_t \{\pi_{t+1}\} \quad \dots(8)$$

$$(\sigma_D + \phi_x + \phi_\pi \kappa_D) \pi_t = \kappa_D \sigma_D E_t \{x_{t+1}\} + (\kappa_D + \beta(\sigma_D + \phi_x)) E_t \{\pi_{t+1}\} \quad \dots(9)$$

The AD and AS (2) and (3) are transformed to (8) and (9), as required for a rational expectations solution, and written in matrix form:

$$\begin{bmatrix} x_t \\ \pi_t \end{bmatrix} = A_T \begin{bmatrix} E_t \{x_{t+1}\} \\ E_t \{\pi_{t+1}\} \end{bmatrix} \quad \dots(10)$$

where

$$A_T \equiv \Omega \begin{bmatrix} \sigma_D & 1 - \beta \phi_\pi \\ \sigma_D \kappa_D & \kappa_D + \beta(\sigma_D + \phi_x) \end{bmatrix} \text{ and } \Omega = \frac{1}{\sigma_D + \phi_x + \kappa_D \phi_\pi}$$

The stability condition<sup>6</sup> for a unique non-explosive solution, to which the forward-looking variables jump, is  $\kappa_D(\phi_\pi - 1) + (1 - \beta)\phi_x > 0$ . A policy response to inflation that exceeds unity is sufficient to ensure stability. The result is qualitatively similar as for the SOE in GM, although the coefficient values are different. GM's  $\kappa$  becomes  $\kappa_D$  in the SOEME;  $\overline{rr}_t$  is also different, subject to larger shocks<sup>7</sup>. The price equation (3) has the implication that in the steady-state, a rise in inflation raises the output gap by  $\frac{(1 - \beta)}{\kappa_D}$ . Then  $\phi_\pi + \frac{(1 - \beta)}{\kappa_D} \phi_x$  gives the long-run response of the policy rate to a persistent rise in inflation. The Taylor principle, which the stability condition satisfies, says this response must exceed unity. In the SOEME, since  $\kappa_D > \kappa$  and is large<sup>8</sup> the permanent rise in policy rate is driven more by  $\phi_\pi$ .

Calibrating the SOEME model required a lagged term in the policy variable to capture slow monetary policy transmission through segmented financial markets<sup>9</sup>. In addition, only a proportion  $\gamma_f < 1$  of firms set prices in a forward-looking manner. The model equation (11) and (12), with these additions, turned out to be stable under discretionary optimization and sensitivity analysis conducted with the parameters as given in Table

6 The stability condition for a two equation difference system is determinant  $A > 0$ , and determinant  $A + \text{trace } A > -1$  when the system is written in the form  $z_t = E(z_{t+1}) + \dots$  (see Woodford, 2003).

7 There can be many reasons for higher shocks to the real interest rate in EMs. Another factor affecting EM interest rates is country risk. Neumeyer and Perri (2005) reproduce EM business cycle stylized facts by introducing large shocks to the real interest rate due to changes in such risk.

8 In the calibrated SOEME for the values given in Table 1  $\kappa_D = 0.47$  so  $(1 - \beta)/\kappa_D = 0.02$ .

9 This differs from different types of lags due to inertia and stabilization objectives analysed in the literature. See, for example Evans and McGough (2005).

1, even where weights on inflation were low in the loss function and in the derived policy reaction function.

The latter gives the final weight on the CB objectives in the calibrations after the constraints, subject to which the optimization is done, are substituted in the policy objective function. A CB reaction function may include more variables than a Taylor rule, but the two are related since a monetary policy rule normally gives the CB's response to current or forecasted macro variables. Given the CB's objective function used, the arguments of the derived reaction function are the same as our estimated monetary policy rule, and differ from the standard Taylor rule in including a lagged interest rate term.

$$x_{t+1} = x_t + \frac{1}{\sigma_D} (0.2r_{t-1} + 0.8r_t - E_t\pi_{H,t+1} - \overline{rr_t}) \quad \dots(11)$$

$$\pi_{H,t+1} = \frac{1}{\gamma_f\beta} \pi_{H,t} - \frac{\lambda}{\gamma_f\beta} (\sigma_D + \phi)x_t - \frac{\gamma_b}{\beta\gamma_f} \pi_{H,t-1} \quad \dots(12)$$

Since a positive smoothing parameter  $q_i$  in the CB loss function reduces the policy response to inflation, some weight on  $\pi$  is required for stability. With  $q_i = 0$  even no weight on inflation generates stable outcomes. For example, if  $q_i = 1$  outcomes are indeterminate with  $q_x = 0$  and  $q_\pi$  less than 1; they are also indeterminate with  $q_x = 0.07$  if  $q_\pi$  less than 0.9; but if  $q_i = 0$  and  $q_x = 0.07$  outcomes are determinate even with  $q_\pi = 0$ . In the estimated reaction functions with varying parameter values in Goyal (2011, Table 4) the weights on inflation range from 4.28 to 0.0091. The lags in the system, and other structural aspects, may be contributing to stability even with a low policy reaction to inflation.

Since the SOEME model under optimal discretionary policy was stable even with a weight on inflation less than unity, we next derive stability conditions for the more complex calibrated SOEME model under a Taylor-type policy rule.

#### 4.1. Stability Conditions for the Calibrated SOEME with a Policy Rule

To solve for stability under a policy rule with the calibrated SOEME model the equations (11) and (12) are written in the form (15) and (16), where expectations of future variables affect current variables, and the policy rule (13) with a generic auto-correlated shock term  $v_t$  (14) substituted in them.

$$r_t = \rho + \phi_\pi \pi_{H,t} + \phi_x x_t + v_t \quad \dots(13)$$

$$v_t = \rho_v v_{t-1} + \varepsilon_t \quad \dots(14)$$

$$x_t = \Omega \sigma_D E_t x_{t+1} + \Omega (1 - 0.8\phi_\pi \gamma_f \beta) E_t \pi_{H,t+1} - \Omega (0.2\phi_\pi + 0.8\phi_\pi \gamma_b) \pi_{H,t-1} - 0.2\phi_x \Omega x_{t-1} - \Omega \rho - 0.8\Omega (\rho_v v_{t-1} + \varepsilon_t) - 0.2\Omega v_{t-1} + \Omega \overline{rr_t} \quad \dots(15)$$

$$\begin{aligned}\pi_{H,t} = & \lambda(\sigma_D + \phi)\Omega\sigma_DE_t x_{t+1} + (\gamma_f\beta + \Omega\lambda(\sigma_D + \phi)(1 - 0.8\phi_\pi\gamma_f\beta))E_t\pi_{H,t+1} - \\ & (\Omega\lambda(\sigma_D + \phi)(0.2\phi_\pi + 0.8\phi_\pi\gamma_b) - \gamma_b)\pi_{H,t-1} - 0.2\phi_x\Omega\lambda(\sigma_D + \phi)x_{t-1} + \\ & \lambda\Omega(\sigma_D + \phi)(\rho + 0.8(\rho_v v_{t-1} + \varepsilon) + 0.2v_{t-1} - \overline{rr_t})\end{aligned}\quad \dots(16)$$

where

$$\Omega = \frac{1}{(\sigma_D + 0.8\phi_x + 0.8\lambda(\sigma_D + \phi)\phi_\pi)}$$

They give the following higher order difference equation system:

$$\text{where } \begin{bmatrix} x_t \\ \pi_{H,t} \end{bmatrix} = A \begin{bmatrix} E_t x_{t+1} \\ E_t \pi_{H,t+1} \end{bmatrix} - B \begin{bmatrix} x_{t-1} \\ \pi_{H,t-1} \end{bmatrix} + \Omega C [r\tilde{r}_t - 0.2v_{t-1} - 0.8\rho v_{t-1}] \quad \dots(17)$$

$$\begin{aligned}A & \equiv \begin{bmatrix} \Omega\sigma_D & \Omega(1 - 0.8\phi_\pi\gamma_f\beta) \\ \lambda(\sigma_D + \phi)\Omega\sigma_D & \gamma_f\beta + \Omega\lambda(\sigma_D + \phi)(1 - 0.8\phi_\pi\gamma_f\beta) \end{bmatrix} \\ B & \equiv \begin{bmatrix} 0.2\phi_x\Omega & \Omega(0.2\phi_\pi + 0.8\phi_\pi\gamma_b) \\ 0.2\phi_x\Omega\lambda(\sigma_D + \phi) & \Omega\lambda(\sigma_D + \phi)(0.2\phi_\pi + 0.8\phi_\pi\gamma_b) - \gamma_b \end{bmatrix}\end{aligned}$$

Consider a second order difference equation:

$$x_{t+2} + ax_{t+1} + bx_t = c_t$$

The solution is stable<sup>10</sup> iff the following correlations are satisfied:

$$\begin{aligned}|a| & < 1+b \\ b & < 1\end{aligned}$$

Rewriting (17) as:

$$\begin{bmatrix} E_t x_{t+1} \\ E_t \pi_{H,t+1} \end{bmatrix} - \frac{1}{A} \begin{bmatrix} x_t \\ \pi_{H,t} \end{bmatrix} - \frac{B}{A} \begin{bmatrix} x_{t-1} \\ \pi_{H,t-1} \end{bmatrix} = C \quad \dots(18)$$

$\frac{1}{A} < 1 - \frac{B}{A}$  and  $-\frac{B}{A} < 1$  will define the stability of the equation.

The first condition can be written as:

$$1 < A - B \quad \dots(19)$$

<sup>10</sup> Stability is discussed in Blanchard and Kahn (1980), Woodford (2003), Gali (2008). Hoy *et al.* (2004, p. 831) list three conditions for the system to be locally unique. These are the two given in the text and a third  $a - b > -1$  which is satisfied trivially.

Since,

$$\begin{aligned} |A| &= \Omega \sigma_D \gamma_f \beta \\ |B| &= -0.2 \phi_x \Omega \gamma_b \\ 1 < A-B &= \frac{1}{\Omega} < \sigma_D \gamma_f \beta + 0.2 \phi_x \gamma_b \end{aligned} \quad \dots(20)$$

The second condition is:

$$-\frac{B}{A} < 1 \quad \dots(21)$$

$$1 < \frac{\sigma_D \gamma_f \beta}{0.2 \phi_x \gamma_b} \quad \dots(22)$$

Condition (22) defines a cap for the weight given to the output gap,  $\phi_x$ , but does not impose any constraint on the weight given to inflation deviation,  $\phi_\pi$ . It gives a high upper bound for  $\phi_x$ .

Condition (20) also defines cap for  $\phi_x$  and for  $\phi_\pi$  since the latter enters  $\Omega$ . The cap for  $\phi_\pi$  is negative unless  $\phi_x$  is negative, and vice versa. Thus for stability the policy rule imposes a negative weight either on inflation deviation from target or on the output gap. Since the caps derived from condition (20), are lower, it is the operative condition.

The stability condition (22) holds but condition (20) is not satisfied for the parameters in Table 1, so while optimization with moderate weights is stable, the Taylor rule is unstable<sup>11</sup>. Combinations of  $\phi_\pi$  and  $\phi_x$  for which both the conditions are satisfied with the benchmark calibrations, with (20) holding just at the margin, are  $\phi_\pi = 2$  and  $\phi_x = -1.5$ , or  $\phi_\pi = -4.2$  and  $\phi_x = 1.6$ . A CB's policy rule is unlikely to have such weights.

#### 4.2. Response to Shocks

Analytically deriving<sup>12</sup> the response to monetary shocks  $v_t$  from the policy rule (13), using the method of undetermined coefficients, gives:

$$\pi_{H,t} = \Theta v_{t-1}, \quad \dots(23)$$

$$\text{where } \Theta = \frac{\Omega(0.2 + 0.8\rho_v)}{\frac{\gamma_f \beta 0.2 \phi_x \Omega}{\lambda(\sigma_D + \phi)} - \frac{\gamma_b \Omega \sigma_D + 1}{\lambda(\sigma_D + \phi)}}$$

<sup>11</sup> In the benchmark optimizing calibrations the upper bound for  $\phi_x$  is 34.1 from condition (22) so this condition is satisfied. However, the lower cap from condition (20), which is not satisfied is -1.5. The cap on  $\phi_\pi$ , -2.3, is also not satisfied.

<sup>12</sup> Derivations are available on request.

$$x_t = \frac{1}{\lambda(\sigma_D + \phi)} (\Theta v_{t-1} - \gamma_b \Theta v_{t-2} - \gamma_f \beta \Theta v_t) \quad \dots(24)$$

We can now compare the inflation and output responses under the policy rule with the discretionary optimization undertaken in Goyal (2011), using the benchmark parameters of Table 1, and the stable weight combination of  $\phi_\pi = -4.2$  and  $\phi_x = 1.6$ . Under the monetary rule, the fall in inflation (0.0065) is less and output (0.0011) is more compared to optimization. Under optimization, a natural rate shock raises the policy rate by 0.013 and reduces inflation by 0.01 and output by 0.006 in the first period. For a persistent rise in  $v_t$  (monetary tightening) of 0.1 optimization is more effective, but in the same direction as a policy rule. Optimization is not only stable but has a lower output cost.

Key results, supported by analysis and calibrations are: policy lags in the SOEME make it stable under forward-looking optimization for a coefficient of inflation in the loss function that differs from unity. But a forward looking policy rule with realistic weights to the function variables in the objective is not stable under rational expectations.

## 5. ADAPTIVE EXPECTATIONS AND A POLICY RULE

Rigidities and volatility in an EM make it difficult to forecast future variables. Policy-makers and agents typically have adaptive rather than model consistent rational expectations. So next we explore the functioning of a policy rule under such behavior, where current variables are solved based on past variables. Future inflation enters both the AD and AS, but since expectations are formed adaptively there is no overall rational expectations solution. Future variables have to be solved as a function of past variables to analyze stability unlike the form of equations (4) and (5). We examine stability in such a case, with our calibrated SOEME AD and AS, adding a policy rule.

The Lucas critique was agents' anticipation of policy will prevent a unique outcome for traditional Keynesian stabilization, where policy makers raise rates to reduce current demand and output. With our structure of monetary transmission, however, a policy rule delivers a unique equilibrium. In the calibrated SOEME model, with interest rate lags and some forward-looking behavior, the model solved backwards as a function of past data is unstable. Adding a policy rule delivers a unique stable solution, to which the economy converges. But, just as in the forward-looking optimizing SOEME solution, the weights on inflation and output gap deviations have to be less than unity for stability.

The backward-looking system (11) and (12), with the policy rule (13) and (14) substituted in it, is stable if the following conditions are satisfied:

$$1 > -A - B$$

$$1 > A - B \quad \dots(25)$$

where:

$$|A| \equiv \frac{1}{\gamma_f \beta} \left( \sigma_D + 0.8\phi_x + \lambda(\sigma_D + \phi) \left( 0.8\phi_\pi - \frac{2}{\gamma_f \beta} \right) \right) \quad \dots(26)$$

$$|B| \equiv -0.2 \frac{\gamma_b}{\gamma_f \beta} \frac{\phi_x}{\sigma_D} \quad \dots(27)$$

These can be solved to obtain floors and caps on the policy rule weights.

The first condition written as,  $1 > -A - B$ , can be used to derive the floors:

$$\phi_x > \left[ \frac{2\lambda(\sigma_D + \phi)}{\gamma_f \beta} - \lambda(\sigma_D + \phi)0.8\phi_\pi - \sigma_D - \gamma_f \beta \right] \frac{\sigma_D}{0.8\sigma_D + 0.2\gamma_b} \quad \dots(28)$$

$$\phi_\pi > \left[ \frac{2\lambda(\sigma_D + \phi)}{\gamma_f \beta} - \left( 0.8 + 0.2 \frac{\gamma_b}{\sigma_D} \right) \phi_x - \sigma_D - \gamma_f \beta \right] \frac{1}{\lambda(\sigma_D + \phi)0.8} \quad \dots(29)$$

That is, the weights in any policy rule followed must exceed the above values.

The second condition,  $1 > A - B$ , can be used to derive the caps:

$$\phi_x < \left[ \gamma_f \beta + \frac{2\lambda(\sigma_D + \phi)}{\gamma_f \beta} - \lambda(\sigma_D + \phi)0.8\phi_\pi - \sigma_D \right] \frac{\sigma_D}{0.8\sigma_D + 0.2\gamma_b} \quad \dots(30)$$

$$\phi_\pi < \left[ \gamma_f \beta + \frac{2\lambda(\sigma_D + \phi)}{\gamma_f \beta} - \left( 0.8 + \frac{0.2\gamma_b}{\sigma_D} \right) \phi_x - \sigma_D \right] \frac{1}{\lambda(\sigma_D + \phi)0.8} \quad \dots(31)$$

That is, the weights in any policy rule followed must be less than the above values.

The cap conditions are the binding ones. The derivation of the cap conditions with respect to  $\gamma_f$  gives:

$$\frac{\delta \phi_x}{\delta \gamma_f} = \left[ \beta - \frac{2\lambda(\sigma_D + \phi)}{\beta \gamma_f^2} \right] \frac{\sigma_D}{0.8\sigma_D + 0.2\gamma_b} \quad \dots(32)$$

$$\frac{\delta \phi_\pi}{\delta \gamma_f} = \left[ \beta - \frac{2\lambda(\sigma_D + \phi)}{\beta \gamma_f^2} \right] \frac{1}{\lambda(\sigma_D + \phi)0.8} \quad \dots(33)$$

Since the second term in the bracket exceeds unity, these derivatives are negative. So

the weights in the policy rule are decreasing in  $\gamma_f$ , and have to be lower, the larger the share of forward-looking behavior. The derivatives with respect to  $\gamma_b$  are also negative but are much smaller. So the derivatives with respect to  $\gamma_f$ . (32) and (33) have a much larger effect on the caps, as the caps change with  $\gamma_f$ .

For the calibrated (Table 1) value of parameters, if  $\gamma_f = 0.4$  the caps for  $\phi_x$  and  $\phi_\pi$  respectively are 0.5 and 0.35. Estimation of  $\gamma_f$  with Indian data gives 64 percent of firms to be forward-looking (Tripathi and Goyal, 2013). For the economy as a whole, including administered prices and informal sectors,  $\gamma_f$  will be lower, so optimal weights in the policy rule should be lower than the values for  $\gamma_f = 0.4$ . The negative derivative of  $\phi_x$  with respect to  $\phi_\pi$  (34) from the cap condition (30), and vice versa from the cap condition (31), shows if one of them rises, the other must fall. If  $\gamma_f$  rises to 0.8, the caps fall to 0.27 and 0.05 respectively. But at that level of  $\gamma_f$  the rational expectations solution can be expected to be more relevant than the backward-looking one, since behavior will become more forward-looking.

$$\frac{\delta\phi_x}{\delta\phi_\pi} = -\lambda(\sigma_D + \phi) \frac{0.8\sigma_D}{0.8\sigma_D + 0.2\gamma_b} \quad \dots(34)$$

In an EM with delayed transmission of policy rates, stability turns out to be very sensitive to the share of forward-looking behavior. This suggests volatility can be high if policy rules are followed unless weights are kept low. Such a policy rule contributes to stability since it prevents over- or under-shooting of rates due to lagged effect of policy.

We compare our analytical results on the policy response coefficients consistent with stability in EMs with an estimated Indian monetary policy rule. Most EMs follow cautious policies and the estimated Taylor Rules do have low weights as we see for India in the next section.

## 6. ESTIMATED MONETARY POLICY RULE

A monetary policy rule was unstable under a rational expectations solution in the calibrated SOEME. But in the backward-looking solution, stability imposed low caps on both policy rule coefficients. Our results suggest that with different types of lags and rigidities the feedback coefficients required for determinacy can be very different from the Taylor Principle. What do estimated rules show?

There is a large empirical literature estimating the Taylor rule. The original equation was:

$$i_t = \pi_t + r_t^* + \phi_\pi(\pi_t - \pi_t^*) + \phi_x(y_t - \bar{y}_t) \quad \dots(35)$$

where,  $\pi_t^*$  is the desired rate of inflation,  $r_t^*$  is the assumed equilibrium real interest

rate,  $y_t$ , is the logarithm of real GDP, and  $\bar{y}_t$  is the logarithm of potential output, as determined by a linear trend. Taylor proposed setting  $\phi_\pi = \phi_x = 0.5$ . As long as  $\phi_\pi > 0$ , an increase in inflation of one percentage point would lead the CB to raise the nominal interest rate by  $1 + \phi_\pi$ , thus raising the real interest rate. The simple NKE models can imply a very low  $\phi_x$ , since in forward-looking models with demand shocks the feedback to inflation is sufficient to stabilize output<sup>13</sup>.

As the empirical Taylor rule literature developed, the estimated equation was simplified. Either the short policy rate was regressed on the deviation of output from potential and of inflation from target, or a constant term was assumed to include a constant inflation target and real interest rate. So the short policy rate was regressed on inflation, on the deviation of output from potential, and a constant capturing the inflation target. A lagged interest rate was included to capture policy smoothing.

We estimated the latter Taylor rule specification for India to compare its coefficients with our theoretical results, and assess Indian monetary policy. We use data at quarterly frequency from 2000Q2 to 2011Q2. Variables include call or money market rate, GDP, core and headline wholesale price index. All the growth rate and inflation terms are in percentages, following the practice in the literature (Maslowska, 2009). Year-on-year headline inflation is measured as annual percentage change in Wholesale Price Index (WPI). Core inflation is defined as nonfood manufacturing goods inflation, whose share was around 52.2 percent in WPI. All the variables are tested for seasonality. Since analysis of linear plots show that quarterly GDP and WPI series have multiplicative seasonality, we de-seasonalize the series using the X-12 ARIMA procedure. We estimate trend or target output using the HP filter, and calculate output gap as the percent deviation of real GDP from a target, as originally proposed by Taylor:

$$y = ((Y - Y^*)/Y^*) * 100$$

where  $Y$  is real GDP (proxied by the industrial production index), and  $Y^*$  is trend real GDP given by HP filter.

Augmented Dickey-Fuller unit root tests show the variables are stationary. The Durbin Watson test indicates serial correlation and the Breusch-Pagan test shows heteroskedasticity in the error terms. To correct for both autocorrelation and heteroskedasticity, we estimate our equation using ordinary least squares with Newey-West variance-covariance matrix.

13 The NKE literature calls it the 'divine coincidence' when the CB does not need to take fluctuations in the output gap into account when setting interest rates. While his work supported the Taylor Principle, Woodford's (2001) differences with the empirical Taylor rule were: First, the welfare theoretic loss function implies the inflation target should be zero in the pure frictionless model. Second, the output gap should be calculated using the natural output, not the past deterministic trend. All the shocks, such as technology, and world income, that affect the natural interest rate in equation (2) affect the natural output. In the SOEME these shocks include consumption of the P-type. See Goyal (2009) for more details on natural output in a SOEME.

The two estimated equations for headline inflation and core inflation (t-values in brackets) are as follows:

Headline inflation

$$r_t = 1.85 + 0.58r_{t-1} + 0.156\pi_t + 0.32y_t$$

(2.71)      (5.24)      (2.83)      (3.12)

Core inflation

$$r_t = 2.12 + 0.59r_{t-1} + 0.126\pi_t + 0.29y_t$$

(2.96)      (5.21)      (2.06)      (2.93)

These imply the long-run rise in  $r_t$  due to a persistent rise in inflation is 0.16 and 0.13 respectively. The long-run response is given by  $\phi_\pi + \frac{(1-\beta)}{\kappa_D}\phi_x$ .

The coefficients are of a similar order of magnitude to the reaction functions estimated in the discretionary optimization and to the cap for  $\phi_\pi$  in the policy rule with  $\gamma_f$  of 0.5 to 0.6 of the backward-looking case<sup>14</sup>. The results suggest the implicit policy rule Indian policy makers followed in this period was near optimal. The response to both inflation and the output gap was not high, but the weight on the output gap exceeded that on inflation.

## 7. CONCLUSION

The NKE literature shows that a response to inflation of above unity can impose stability in optimizing models with rational expectations. Theoretical stability results turn out to be the same in an NKE DSGE model adapted to an open economy EM model with two types of agents to capture heterogeneity in labour markets and among consumers. Most estimated EM Taylor rules, including ours in this paper, however, give a coefficient for inflation of much below unity.

Consistent with this, in the calibrated model that has lagged policy rates in the aggregate demand equation, the derived stability condition does not imply the Taylor Principle. A policy rule is unstable in a rational expectations equilibrium. In a backward-looking solution, stability requires low weights on both objectives. As the weight on one rises that on the other should fall. The weight on the output gap exceeds that on inflation deviations. Discretionary forward-looking optimization is also stable. The reaction functions estimated in optimizing simulations and caps from the data driven policy rule are low and consistent with estimated coefficients of Taylor-type rules for India. Discretionary optimization outperforms a policy rule under rational expectations. A policy rule can be followed to the extent backward-looking behavior dominates, but with weights on the

14 With the benchmark parameters,  $\phi_x = 0.3$  and  $\gamma_f = 0.6$  the cap is 0.11 for  $\phi_\pi$ .

arguments of less than unity. It would implement standard macroeconomic stabilization while preventing overshooting of rates.

Analytical solutions to monetary policy shocks using the calibrated equations, serve as consistency checks, and give results similar to the discretionary optimization. Therefore, a key result, supported by analysis, calibration and estimations is: lags and rigidities in the SOEME make it stable for low weights on inflation, in Central Bank loss functions, optimizing reaction functions, as well as a smoothed policy rule.

Outcomes are stable even with a weight of zero on inflation in the loss function when there is no weight on interest rate smoothing, and weights on inflation in estimated reaction functions can be very low. The lags in the system, and other structural aspects, may be contributing to stability even with a low policy reaction to inflation. Such low coefficients may be necessary to prevent instrument instability in the presence of lagged policy transmission when backward-looking behavior dominates. A policy rule delivers a unique saddle stable equilibrium in an adaptive expectations equilibrium. It follows that if an EM follows a policy rule it should ensure coefficients are low, until monetary transmission matures and the share of forward-looking behavior rises. During the transition, discretionary optimization may give more flexibilities.

The results suggest, more generally, that the effect of specific rigidities on stability should be more carefully explored, and the knowledge of these rigidities can give useful inputs for the design of policy.

#### REFERENCES

- Blanchard, O.J. and Kahn, C.M. (1980), The Solution of Linear Difference Models under Rational Expectations, *Econometrica*, Vol. 48, 1305–1311.
- Bullard, J. and Mitra, K. (2007), Determinacy, Learnability, and Monetary Policy Inertia, *Journal of Money, Credit and Banking*, Vol. 39, 1177–1212.
- Bullard, J. and Mitra, K. (2002), Learning About Monetary Policy Rules, *Journal of Monetary Economics*, Vol. 49, 1105–1129.
- Clarida R., Galí, J. and Gertler, M. (2000), Monetary Policy Rules and Macroeconomic Stability: Evidence and Some Theory, *Quarterly Journal of Economics*, Vol. 115, 147–180.
- Clarida R., Galí, J. and Gertler, M. (1999), The Science of Monetary Policy: A New Keynesian Perspective, *Journal of Economic Literature*, Vol. 37, 1661–707.
- Cochrane, J.H. (2011), Determinacy and Identification with Taylor Rules, *Journal of Political Economy*, Vol. 119, 565–615.
- Duffy, J. and Xiao, W. (2007), The Value of Interest Rate Stabilization Policies when Agents are Learning, *Journal of Money, Credit and Banking*, Vol. 39, 2041–2056.
- Evans, G. and Honkapohja, S. (2003), Expectations and the Stability Problem for Optimal Monetary Policies, *Review of Economic Studies*, Vol. 70, 807–824.

- Evans, G. and McGough, B. (2005), Monetary Policy and Stable Indeterminacy with Inertia, *Economics Letters*, Vol. 87, 1-7.
- Friedman, B.M. (1990), Targets and Instruments of Monetary Policy, In B. Friedman and F. Hahn (eds.), *The Handbook of Monetary Economics*, New York: North Holland, Vol. 2, 1183-1230.
- Galí, J. (2008), *Monetary Policy, Inflation, and the Business Cycle: An Introduction to the New Keynesian Framework*, NJ: Princeton University Press.
- Galí J., López-Salido, J.D. and Vallés, J. (2004), Rule of Thumb Consumers and the Design of Interest Rates Rules, *Journal of Money, Credit, and Banking*, Vol. 36, 739-764.
- Galí, J. and Monacelli, T. (2005), Monetary Policy and Exchange Rate Volatility in a Small Open Economy, *Review of Economic Studies*, Vol. 72, 707-734.
- Goyal, A. (2011), A General Equilibrium Open Economy Model for Emerging Markets: Monetary Policy with a Dualistic Labor Market, *Economic Modelling*, Vol. 28, 1392-1404.
- Goyal, A. (2009), The Natural Interest Rate in Emerging Markets, In: B. Dutta, T. Roy, and E. Somanathan (eds.), *New and Enduring Themes in Development Economics*, World Scientific Publishers.
- Goyal, A. (2007), Trade-offs, Delegation and Fiscal-Monetary Coordination in a Developing Economy, *Indian Economic Review*, Vol. 42, 141-164.
- Hoy, M., Livernois, J., McKenna, C., Rees, R. and Stengos, T. (2004), *Mathematics for Economists*, Second Edition. New Delhi: Prentice Hall of India.
- Maslowska, A. (2009), Using Taylor Rule to Explain Institutional Changes in Central Banks, *Aboa Centre for Economics*, Discussion Paper 46.
- McCallum, B.T. (1981), Price Level Determinacy with an Interest Rate Policy Rule and Rational Expectations, *Journal of Monetary Economics*, Vol. 8, 319-329.
- Neumeyer, P.A. and Perri, F. (2005), Business Cycles in Emerging Economies: The Role of Interest Rates, *Journal of Monetary Economics*, Vol. 52, 345-380.
- Sargent, T.J. and Wallace, N. (1975), Rational Expectations, the Optimal Monetary Instrument, and the Optimal Money Supply Rule, *Journal of Political Economy*, Vol. 83, 241-254.
- Taylor, J.B. (1993), Discretion versus Policy Rules in Practice, *Carnegie-Rochester Conference Series on Public Policy*, Vol. 39, 195-214.
- Taylor, J.B. (2001), The Role of the Exchange Rate in Monetary Policy Rules, *American Economic Review*, Papers and Proceedings, Vol. 91, 263-267.
- Tripathi, S. and Goyal, A. (2013), Relative Prices, the Price Level and Inflation: Effects of Asymmetric and Sticky Adjustment, *IUP Journal of Applied Economics*, Vol. 12, 41-61.
- Woodford, M. (2003), *Interest and Prices: Foundations of a Theory of Monetary Policy*, NJ: Princeton University Press.
- Woodford, M. (2001), The Taylor Rule and Optimal Monetary Policy, *American Economic Review*, Vol. 91, 232-237.